
Professor Xiaoming Yuan

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**Multi-timescale dynamic issues of power
electronised power systems and multi-
scale magnitude-phase dynamic theory**

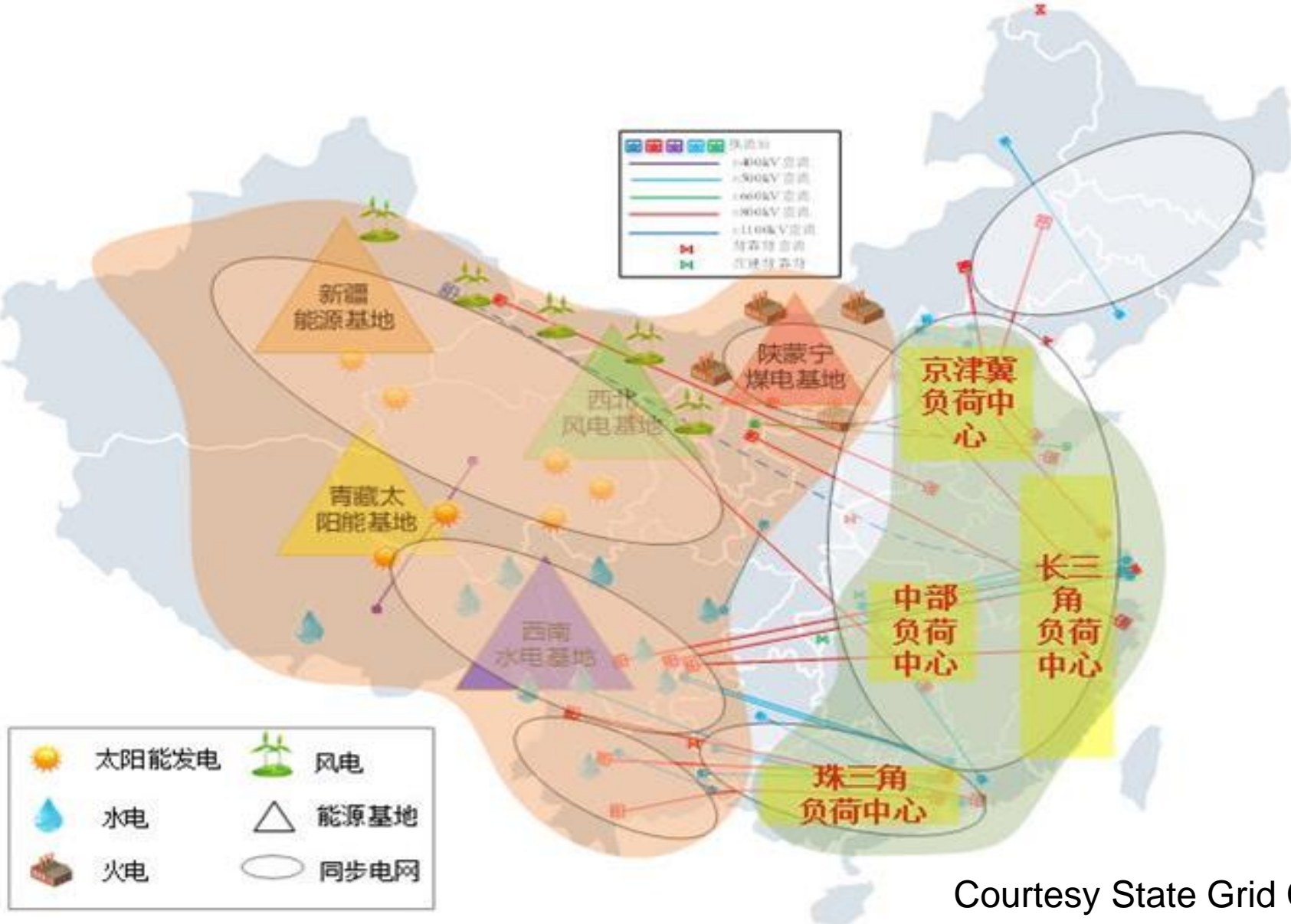
Amplitude-Phase Dynamics

A Theory for Power Electronics Based Power Systems Dynamics

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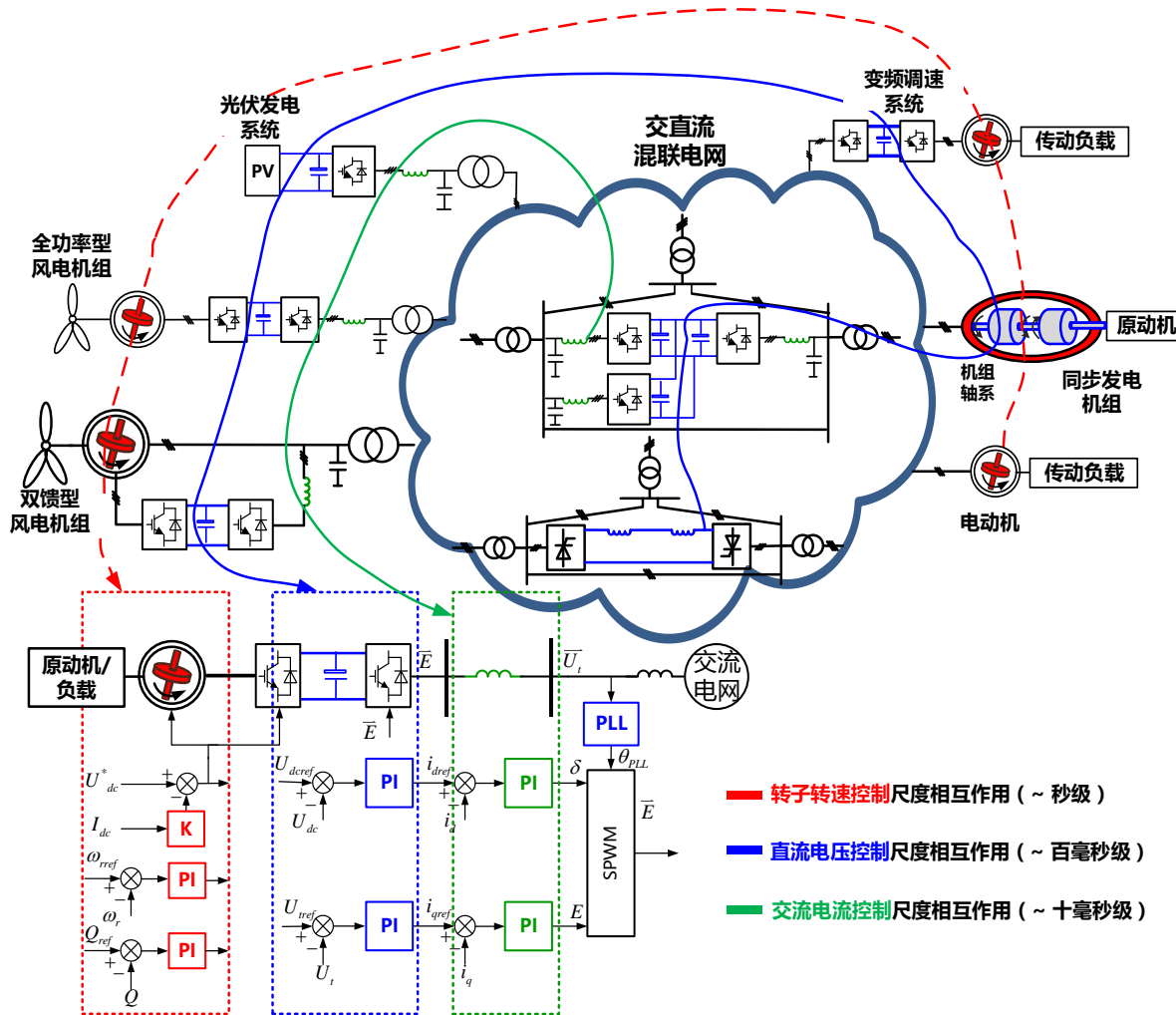
July 5, 2018

Grid China: Machines to Power Electronics



Courtesy State Grid China

System Dynamics: New Scenario



Dynamical behavior: machines and power electronics

Operating the system: simulation and mechanism

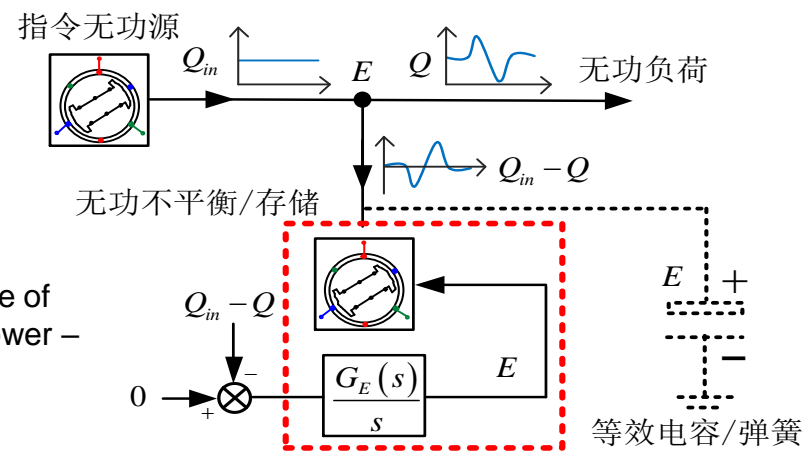
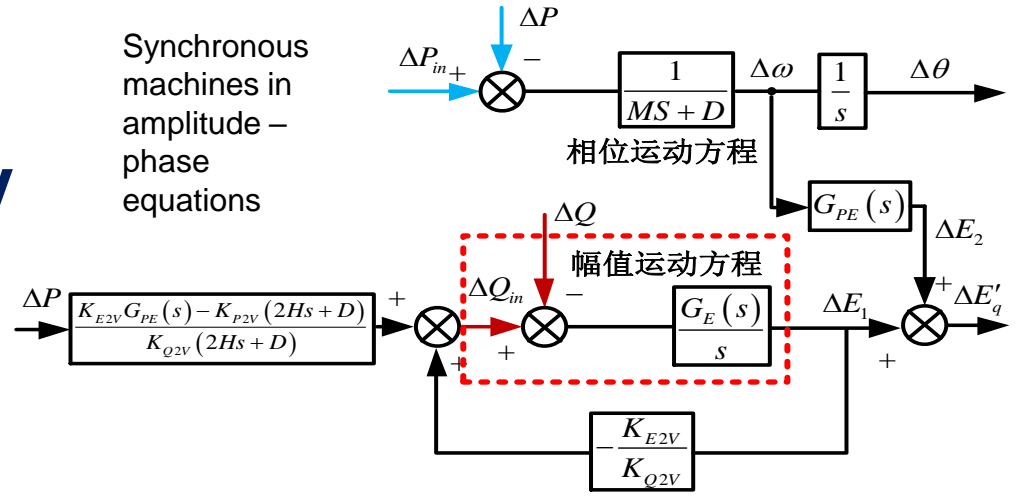
- **Concepts for Understanding Characteristics**
- **Methodologies for Analyzing Dynamics**

Amplitude-Phase Equations for Nodes

Power balancing
excitation – internal
voltage response key
I/O factors

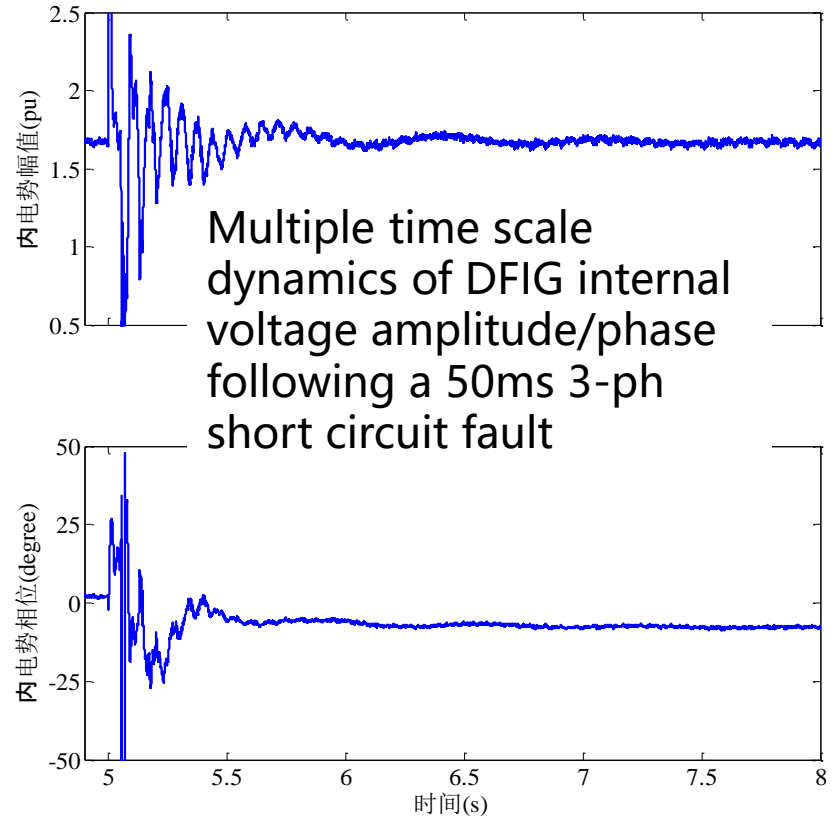
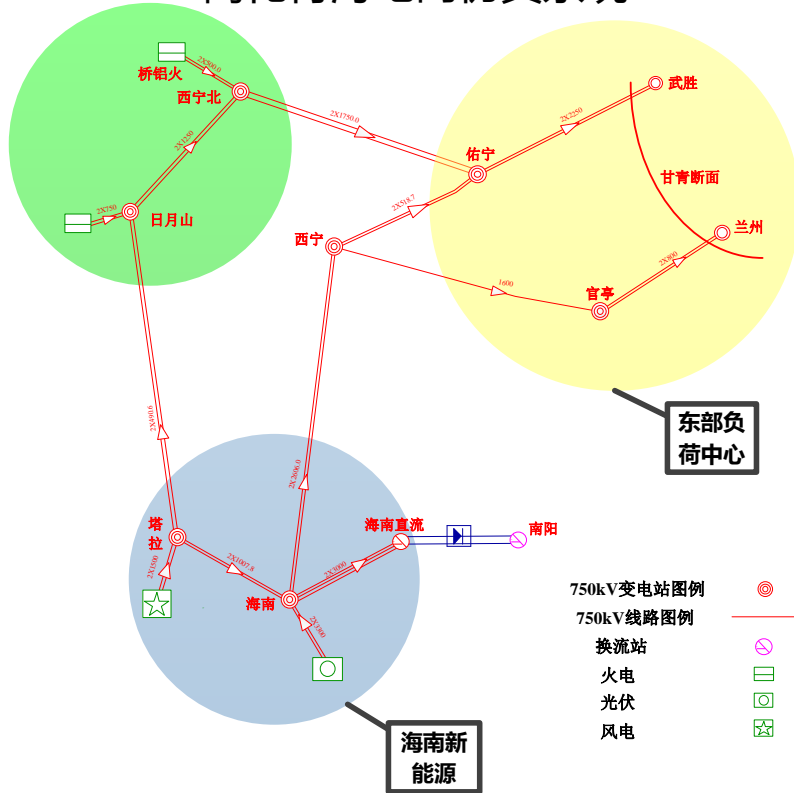
Mathematics and
physics
(mass/spring/damping)
of relations

Properties and laws
governing the
relations



Multi-time scale controlled characteristics

简化青海电网仿真系统



From single time scale, low order, linear, continuous, decoupled system of synchronous machines to multi time scale, high order, non-linear, switching, coupled system of power electronics converters

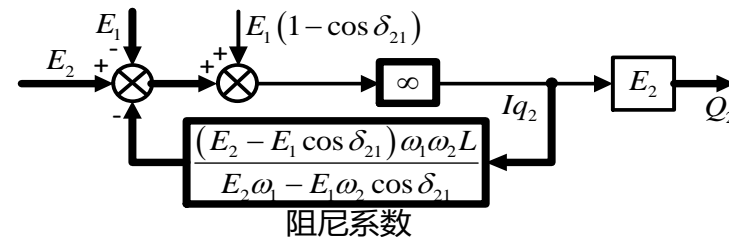
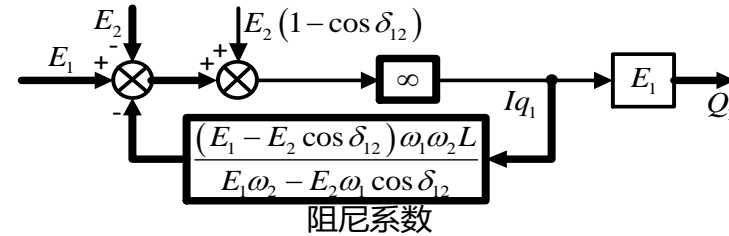
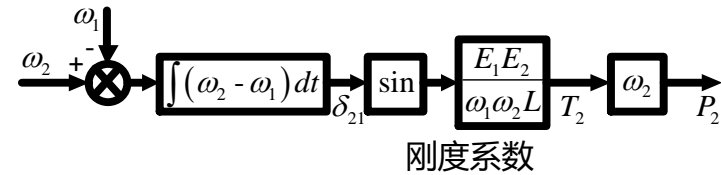
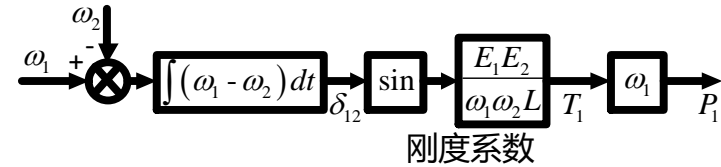
Amplitude–Phase Equations for Networks



Internal voltage excitation – power balancing response
key I/O factors

Mathematics and physics
(mass/spring/damping)
of the relations

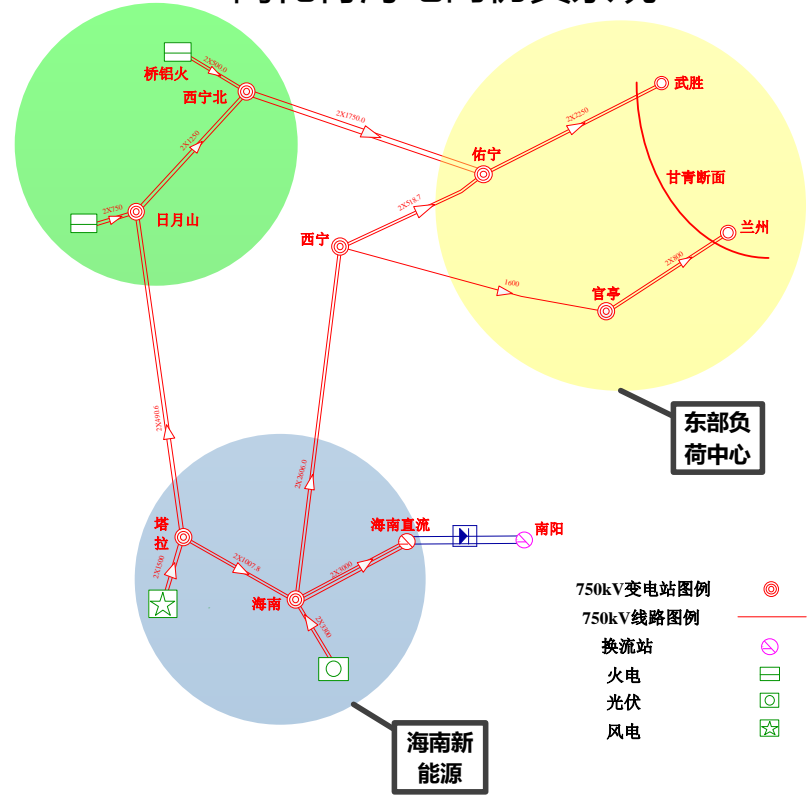
Properties and laws governing the relations



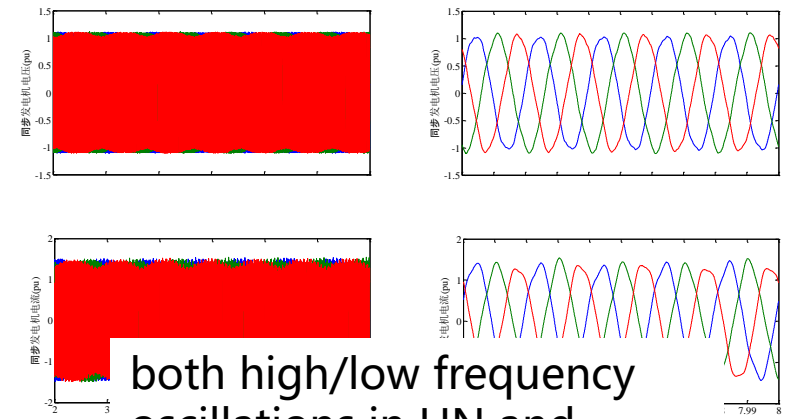
Multi-time scale excited characteristics



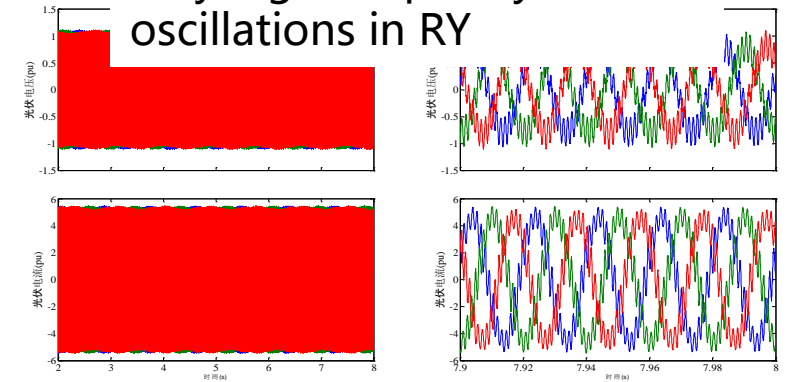
简化青海电网仿真系统



节点电压电流波形
日月山火电



节点电压电流波形
海南光伏发电



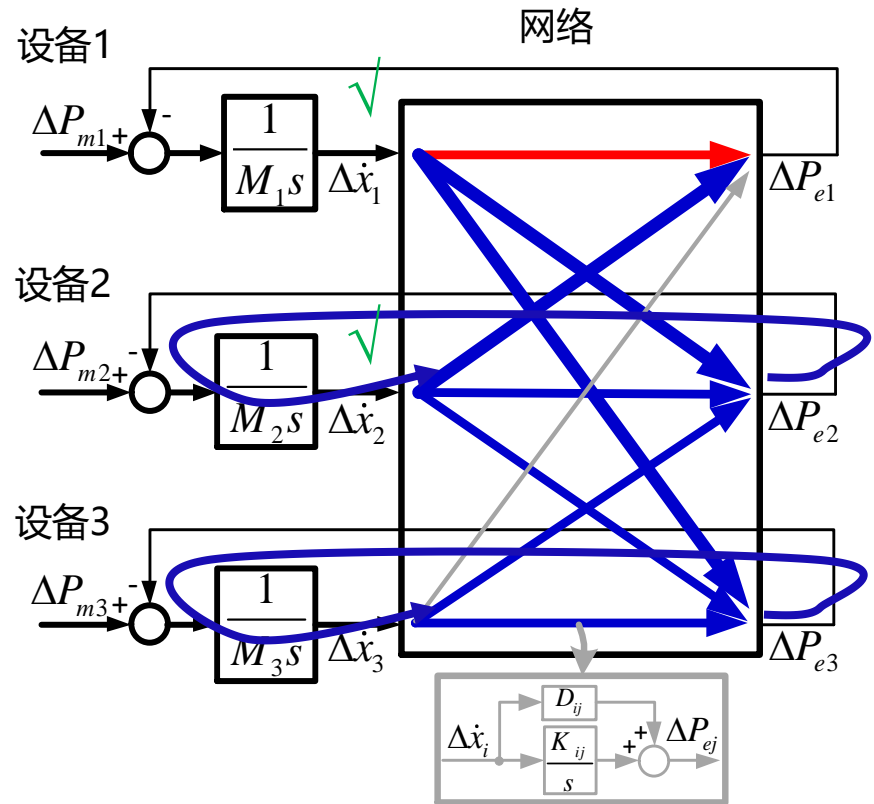
From single time scale, static, nonlinear system under synchronous machine excitation to multiple time scale, dynamic, nonlinear system under power electronics excitation

Stabilization Paths for Interactions

Cross-coupled paths between power balancing and internal voltage of machines

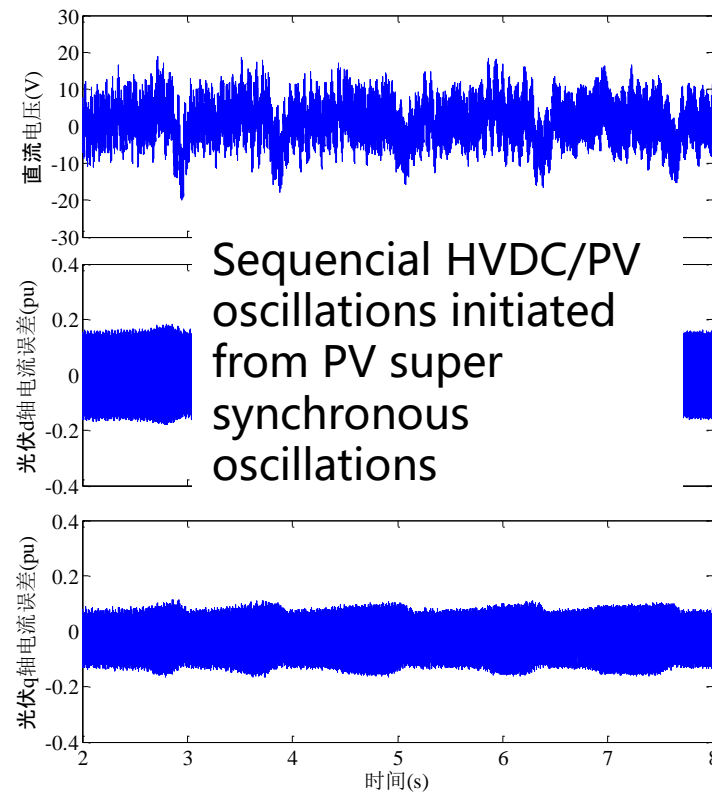
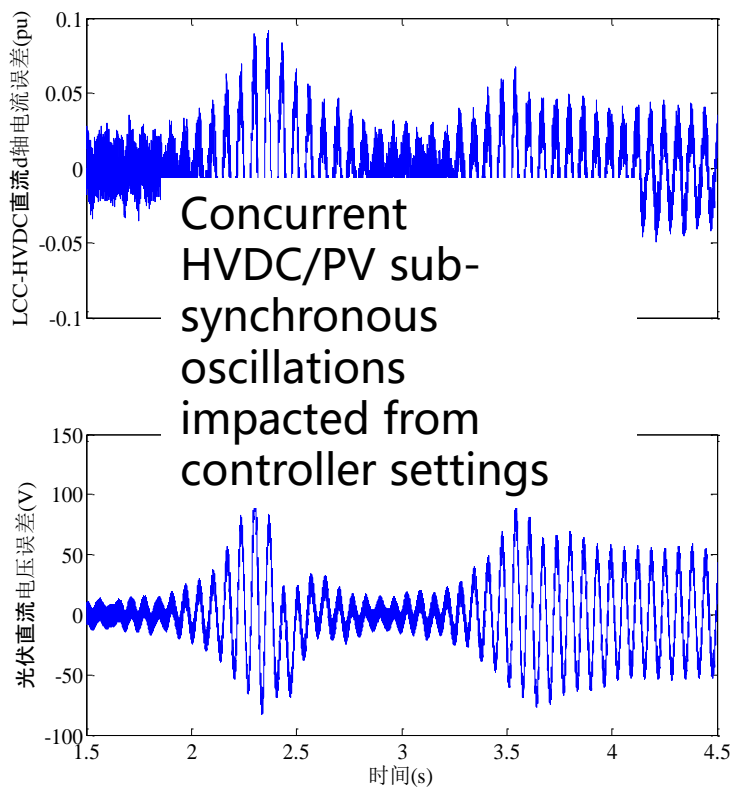
Mathematics and physics of the interaction relations

Properties and laws governing the interaction relations



En-stabilizing paths of machine 2 to machine 1 following disturbance to machine 1

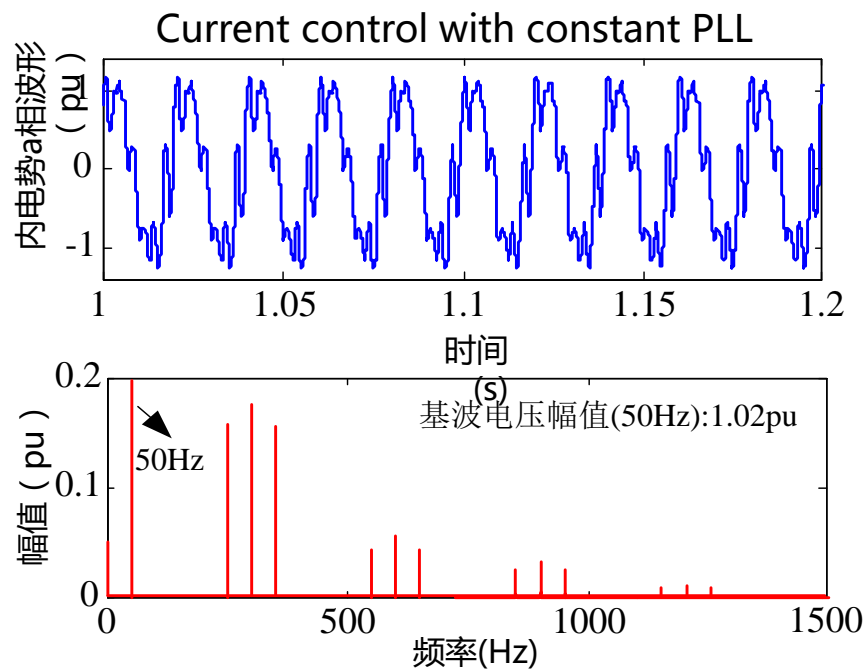
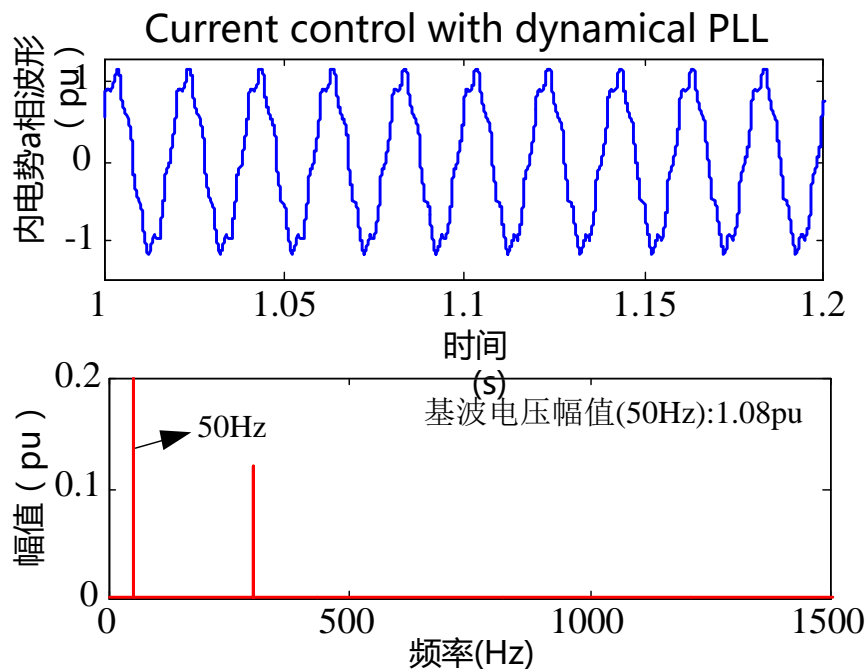
Sequential and Concurrent Interactions



From only intra-time scale **concurrent** interactions to also inter-time scale **sequential** interactions

- **Concepts for Understanding Characteristics**
- **Methodologies for Analyzing Dynamics**

Internal voltage dynamics – harmonics vs. modulation

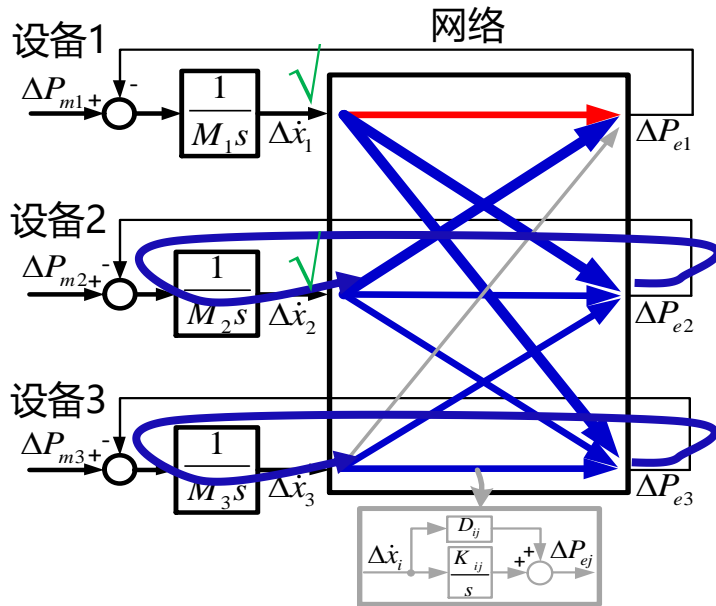


Amplitude/frequency modulated signal – integration/differentiation

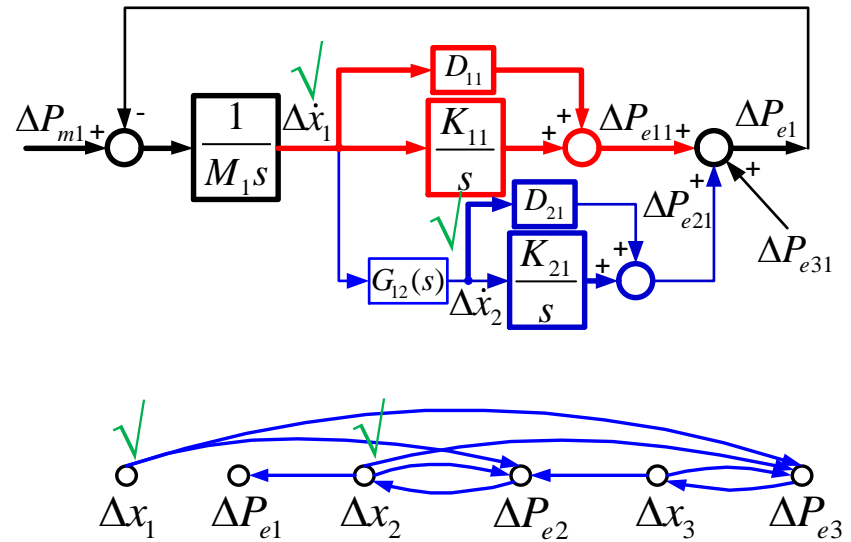
$$\int_{t_0}^t A(t) \cos\left(\int \omega(t) dt\right) dt = \int_{t_0}^t \frac{A(t)}{\omega(t)} d \sin\left(\int \omega(t) dt\right) = \frac{A(t)}{\omega(t)} \sin\left(\int \omega(t) dt\right) \Big|_{t_0}^t - \int_{t_0}^t \sin\left(\int \omega(t) dt\right) d \frac{A(t)}{\omega(t)}$$

Open Loop Interaction Path Analysis

interaction path of machine 2 to 1 following disturbance to 1



simplified signal flow for a two-machine system



balancing equation
(machine 1)

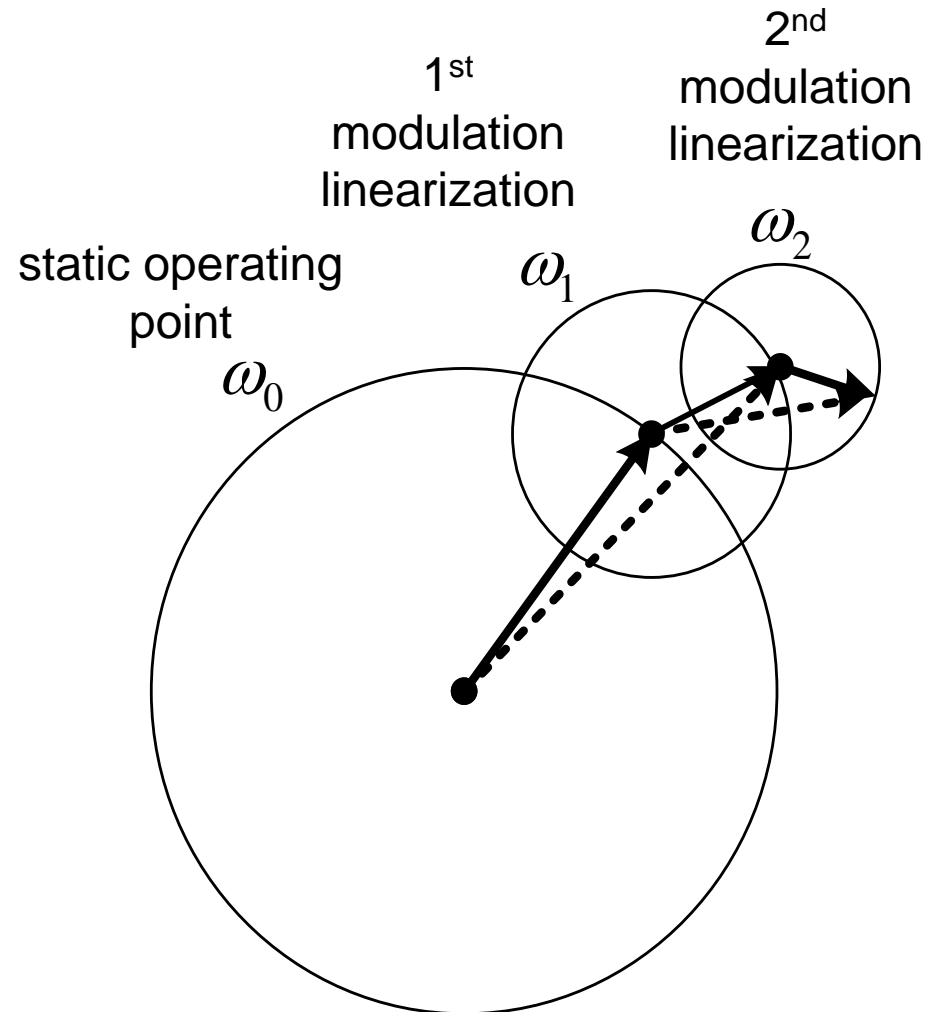
$$M_1 \ddot{x}_1 + (D_{11} \dot{x}_1 + \underline{D_{21} \dot{x}_2} + D_{31} \dot{x}_3) + (K_{11} x_1 + K_{21} x_2 + K_{31} x_3) = 0$$

equivalent balancing
equation

$$M_1 \ddot{x}_1 + (D_{11} + \underline{G_{12}(s) D_{21}} + G_{13}(s) D_{31}) \dot{x}_1 + (K_{11} + G_{12}(s) K_{21} + G_{13}(s) K_{31}) x_1 = 0$$

Linearize the system at its current operating point when mode from the last linearization twists

Iterative modulation of last linear mode forms non-linear mode of system



Modeling and characterization from structure and mathematics based to function and mechanism based, universal approach to characterize nodes, networks and their interactions in systems

State pattern and linearization from varying sinusoidal and its harmonics to constant amplitude/frequency and its modulation, modulation vs. harmonics linearization, milestone approach for AC systems

MIMO system analysis from matrix/mathematics based oscillation mode analysis to SISO/mechanism based interaction path analysis, toward essence of interactions and roles in system dynamics

Non-linear system analysis from simulation to analytical based solutions, via iterative modulation linearization, milestone foundation to nonlinear system dynamics